



Advanced Mathematical Decision Making (AMDM)





Advanced Mathematical Decision Making (AMDM) Teaching & Learning Framework

Semester 1				Semester 2		
Unit 1 4 weeks	Unit 2 5 weeks	Unit 3 7 weeks	Unit 4 5 weeks	Unit 5 4 weeks	Unit 6 6 weeks	Unit 7 5 weeks
Analyzing Numerical Data	Probability	Statistical Studies	Using Recursion in Models & Decision Making	Using Functions in Models & Decision Making	Decision Making in Finance	Networks & Graphs
<p>MAMDMN1. Students will extend the understanding of proportional reasoning, ratios, rates, and percents by applying them to various settings to include business, media, and consumerism.</p> <p>a. Use proportional reasoning to solve problems involving ratios.</p> <p>b. Understand and use averages, weighted averages, and indices.</p> <p>c. Solve problems involving large quantities that are not easily measured.</p> <p>d. Understand how identification numbers, such as UPCs, are created and verified.</p>	<p>MAMDMD1. Students will determine probability and expected value to inform everyday decision making.</p> <p>a. Determine conditional probabilities and probabilities of compound events to make decisions in problem situations.</p> <p>b. Use probabilities to make and justify decisions about risks in everyday life.</p> <p>c. Calculate expected value to analyze mathematical fairness, payoff, and risk.</p>	<p>MAMDMD2. Students will build the skills and vocabulary necessary to analyze and critique reported statistical information, summaries, and graphical displays.</p> <p>MAMDMD3. Students will apply statistical methods to design, conduct, and analyze statistical studies.</p>	<p>MAMDMD4. Students will use functions to model problem situations in both discrete and continuous relationships.</p> <p>a. Determine whether a problem situation involving two quantities is best modeled by a discrete (pattern identification, population growth, compound interest) or continuous (medication dosage, climate change, bone decay) relationship.</p> <p>b. Use linear, exponential, logistic, piecewise and sine functions to construct a model.</p> <p>MAMDMG1. Students will create and use two- and three-dimensional representations of authentic situations.</p> <p>MAMDMG2. Students will solve geometric problems involving inaccessible distances using basic trigonometric principles, including the Law of Sines and the Law of Cosines.</p>	<p>MAMDMD4. Students will use functions to model problem situations in both discrete and continuous relationships.</p> <p>a. Determine whether a problem situation involving two quantities is best modeled by a discrete (pattern identification, population growth, compound interest) or continuous (medication dosage, climate change, bone decay) relationship.</p> <p>b. Use linear, exponential, logistic, piecewise and sine functions to construct a model.</p> <p>MAMDMG1. Students will create and use two- and three-dimensional representations of authentic situations.</p> <p>MAMDMG2. Students will solve geometric problems involving inaccessible distances using basic trigonometric principles, including the Law of Sines and the Law of Cosines.</p>	<p>MAMDMA3. Students will create and analyze mathematical models to make decisions related to earning, investing, spending, and borrowing money.</p> <p>a. Use exponential functions to model change in a variety of financial situations.</p> <p>b. Determine, represent, and analyze mathematical models for income, expenditures, and various types of loans and investments.</p>	<p>MAMDMA2. Students will use a variety of network models to organize data in quantitative situations, make informed decisions, and solve problems.</p> <p>a. Solve problems represented by a vertex-edge graph, and find critical paths, Euler paths, and minimal spanning trees.</p> <p>b. Construct, analyze, and interpret flow charts to develop an algorithm to describe processes such as quality control procedures.</p> <p>c. Investigate the scheduling of projects using PERT.</p> <p>d. Consider problems that can be resolved by coloring graphs.</p>

These units were written to build upon concepts from prior units, so later units contain tasks that depend upon the concepts addressed in earlier units. All units will include the Mathematical Practices and indicate skills to maintain.

NOTE: Mathematical standards are interwoven and should be addressed throughout the year in as many different units and tasks as possible in order to stress the natural connections that exist among mathematical topics.



Standards for Mathematical Practice

The Standards for Mathematical Practice describe varieties of expertise that mathematics educators at all levels should seek to develop in their students. These practices rest on important “processes and proficiencies” with longstanding importance in mathematics education. The first of these are the NCTM process standards of problem solving, reasoning and proof, communication, representation, and connections. The second are the strands of mathematical proficiency specified in the National Research Council’s report *Adding It Up*: adaptive reasoning, strategic competence, conceptual understanding (comprehension of mathematical concepts, operations and relations), procedural fluency (skill in carrying out procedures flexibly, accurately, efficiently and appropriately), and productive disposition (habitual inclination to see mathematics as sensible, useful, and worthwhile, coupled with a belief in diligence and one’s own efficacy).

1. Make sense of problems and persevere in solving them.

High school students start to examine problems by explaining to themselves the meaning of a problem and looking for entry points to its solution. They analyze givens, constraints, relationships, and goals. They make conjectures about the form and meaning of the solution and plan a solution pathway rather than simply jumping into a solution attempt. They consider analogous problems, and try special cases and simpler forms of the original problem in order to gain insight into its solution. They monitor and evaluate their progress and change course if necessary. Older students might, depending on the context of the problem, transform algebraic expressions or change the viewing window on their graphing calculator to get the information they need. By high school, students can explain correspondences between equations, verbal descriptions, tables, and graphs or draw diagrams of important features and relationships, graph data, and search for regularity or trends. They check their answers to problems using different methods and continually ask themselves, “Does this make sense?” They can understand the approaches of others to solving complex problems and identify correspondences between different approaches.

2. Reason abstractly and quantitatively.

High school students seek to make sense of quantities and their relationships in problem situations. They abstract a given situation and represent it symbolically, manipulate the representing symbols, and pause as needed during the manipulation process in order to probe into the referents for the symbols involved. Students use quantitative reasoning to create coherent representations of the problem at hand; consider the units involved; attend to the meaning of quantities, not just how to compute them; and know and flexibly use different properties of operations and objects.

3. Construct viable arguments and critique the reasoning of others.

High school students understand and use stated assumptions, definitions, and previously established results in constructing arguments. They make conjectures and build a logical progression of statements to explore the truth of their conjectures. They are able to analyze situations by breaking them into cases, and can recognize and use counterexamples. They justify their conclusions, communicate them to others, and respond to the arguments of others. They reason inductively about data, making plausible arguments that take into account the context from which the data arose. High school students are also able to compare the effectiveness of two plausible arguments, distinguish correct logic or reasoning from that which is flawed, and—if there is a flaw in an argument—explain what it is. High school students learn to determine domains to which an argument applies, listen or read the arguments of others, decide whether they make sense, and ask useful questions to clarify or improve the arguments.



Standards for Mathematical Practice (continued)

4. Model with mathematics.

High school students can apply the mathematics they know to solve problems arising in everyday life, society, and the workplace. By high school, a student might use geometry to solve a design problem or use a function to describe how one quantity of interest depends on another. High school students making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later. They are able to identify important quantities in a practical situation and map their relationships using such tools as diagrams, two-way tables, graphs, flowcharts and formulas. They can analyze those relationships mathematically to draw conclusions. They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose.

5. Use appropriate tools strategically.

High school students consider the available tools when solving a mathematical problem. These tools might include pencil and paper, concrete models, a ruler, a protractor, a calculator, a spreadsheet, a computer algebra system, a statistical package, or dynamic geometry software. High school students should be sufficiently familiar with tools appropriate for their grade or course to make sound decisions about when each of these tools might be helpful, recognizing both the insight to be gained and their limitations. For example, high school students analyze graphs of functions and solutions generated using a graphing calculator. They detect possible errors by strategically using estimation and other mathematical knowledge. When making mathematical models, they know that technology can enable them to visualize the results of varying assumptions, explore consequences, and compare predictions with data. They are able to identify relevant external mathematical resources, such as digital content located on a website, and use them to pose or solve problems. They are able to use technological tools to explore and deepen their understanding of concepts.

6. Attend to precision.

High school students try to communicate precisely to others by using clear definitions in discussion with others and in their own reasoning. They state the meaning of the symbols they choose, specifying units of measure, and labeling axes to clarify the correspondence with quantities in a problem. They calculate accurately and efficiently, express numerical answers with a degree of precision appropriate for the problem context. By the time they reach high school they have learned to examine claims and make explicit use of definitions.

7. Look for and make use of structure. By high school, students look closely to discern a pattern or structure. In the expression $x^2 + 9x + 14$, older students can see the 14 as 2×7 and the 9 as $2 + 7$. They recognize the significance of an existing line in a geometric figure and can use the strategy of drawing an auxiliary line for solving problems. They also can step back for an overview and shift perspective. They can see complicated things, such as some algebraic expressions, as single objects or as being composed of several objects. For example, they can see $5 - 3(x - y)^2$ as 5 minus a positive number times a square and use that to realize that its value cannot be more than 5 for any real numbers x and y . High school students use these patterns to create equivalent expressions, factor and solve equations, and compose functions, and transform figures.

8. Look for and express regularity in repeated reasoning.

High school students notice if calculations are repeated, and look both for general methods and for shortcuts. Noticing the regularity in the way terms cancel when expanding $(x - 1)(x + 1)$, $(x - 1)(x^2 + x + 1)$, and $(x - 1)(x^3 + x^2 + x + 1)$ might lead them to the general formula for the sum of a geometric series. As they work to solve a problem, derive formulas or make generalizations, high school students maintain oversight of the process, while attending to the details. They continually evaluate the reasonableness of their intermediate results.



Number and Operations

Students will extend their understanding and use of ratios, proportions to solve problems involving in decision making.

MAMDMN1. Students will extend the understanding of proportional reasoning, ratios, rates, and percent by applying them to various settings to include business, media, and consumerism.

- a. Use proportional reasoning to solve problems involving ratios.
- b. Understand and use averages, weighted averages, and indices.
- c. Solve problems involving large quantities that are not easily measured.
- d. Understand how identification numbers, such as UPCs, are created and verified.

Algebra

Students will explore the applications of functions, their characteristics and their use in modeling. Vectors and matrices are employed for solving problems.

MAMDMA1. Students will use vectors and matrices to organize and describe problem situations.

- a. Represent situations and solve problems using vectors in areas such as transportation, computer graphics, and the physics of force and motion.
- b. Represent geometric transformations and solve problems using matrices in fields such as computer animations.

MAMDMA2. Students will use a variety of network models to organize data in quantitative situations, make informed decisions, and solve problems.

- a. Solve problems represented by a vertex-edge graph, and find critical paths, Euler paths, and minimal spanning trees.
- b. Construct, analyze, and interpret flow charts to develop an algorithm to describe processes such as quality control procedures.
- c. Investigate the scheduling of projects using PERT.
- d. Consider problems that can be resolved by coloring graphs.

MAMDMA3. Students will create and analyze mathematical models to make decisions related to earning, investing, spending, and borrowing money.

- a. Use exponential functions to model change in a variety of financial situations.
- b. Determine, represent, and analyze mathematical models for income, expenditures, and various types of loans and investments.

MAMDMA4. Students will analyze and evaluate the mathematics behind various methods of voting and selection.

- a. Evaluate various voting and selection processes to determine an appropriate method for a given situation.
- b. Apply various ranking algorithms to determine an appropriate method for a given situation



Geometry

Students apply tools to model geometric situations and solve problems. Students extend their knowledge of right triangle trigonometry.

MAMDMD1. Students will create and use two- and three-dimensional representations of authentic situations.

MAMDMD2. Students will solve geometric problems involving inaccessible distances using basic trigonometric principles, including the Law of Sines and the Law of Cosines.

Data Analysis and Probability

Students will explore representations of data and models of data as tools in the decision making.

MAMDMD1. Students will determine probability and expected value to inform everyday decision making.

- a. Determine conditional probabilities and probabilities of compound events to make decisions in problem situations.
- b. Use probabilities to make and justify decisions about risks in everyday life.
- c. Calculate expected value to analyze mathematical fairness, payoff, and risk.

MAMDMD2. Students will build the skills and vocabulary necessary to analyze and critique reported statistical information, summaries, and graphical displays.

MAMDMD3. Students will apply statistical methods to design, conduct, and analyze statistical studies.

MAMDMD4. Students will use functions to model problem situations in both discrete and continuous relationships.

- a. Determine whether a problem situation involving two quantities is best modeled by a discrete (pattern identification, population growth, compound interest) or continuous (medication dosage, climate change, bone decay) relationship.
- b. Use linear, exponential, logistic, piecewise and sine functions to construct a model.

Terms/Symbols: Networks, weighted average, indices, vector, critical path, Euler path, minimal spanning trees, PERT, Law of Sines, Law of Cosines, payoff, risk, discrete, continuous, logistics, annuity, future value, present value, ranking, margin of error, cyclical, period, amplitude, phase shift, commission, salary, perpetuity, electoral college, periodic functions, statistical bias.