Clarification of Standards for Parents
Grade 4 Mathematics Unit 4

Dear Parents,

We want to make sure that you have an understanding of the mathematics your child will be learning this year. Below you will find the standards we will be learning in Unit Four. Each standard is in bold print and underlined and below it is an explanation with student examples. Your child is not learning math the way we did when we were in school, so hopefully this will assist you when you help your child at home. Please let your teacher know if you have any questions. 😊

MGSE4.NF.3 Understand a fraction a/b with a > 1 as a sum of fractions 1/b.

a. Understand addition and subtraction of fractions as joining and separating parts referring to the same whole.

A fraction with a numerator of one is called a unit fraction. When students investigate fractions other than unit fractions, such as 2/3, they should be able to join (compose) or separate (decompose) the fractions of the same whole.

Example: \( \frac{2}{3} = \frac{1}{3} + \frac{1}{3} \)

Being able to visualize this decomposition into unit fractions helps students when adding or subtracting fractions. Students need multiple opportunities to work with mixed numbers and be able to decompose them in more than one way. Students may use visual models to help develop this understanding.

Example: \( 1 \frac{1}{4} - \frac{3}{4} = ? \rightarrow \frac{4}{4} + \frac{1}{4} = \frac{5}{4} \rightarrow \frac{5}{4} - \frac{3}{4} = \frac{2}{4} \) or \( \frac{1}{2} \)

Example of word problem:

Mary and Lacey decide to share a pizza. Mary ate \( \frac{3}{6} \) and Lacey ate \( \frac{2}{6} \) of the pizza. How much of the pizza did the girls eat together?

Possible solution: The amount of pizza Mary ate can be thought of as \( \frac{3}{6} \) or \( \frac{1}{6} + \frac{1}{6} + \frac{1}{6} \). The amount of pizza Lacey ate can be thought of as \( \frac{2}{6} \) or \( \frac{1}{6} + \frac{1}{6} \). The total amount of pizza they ate is \( \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6} \) or \( \frac{4}{6} \) of the pizza.

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b. Decompose a fraction into a sum of fractions with the same denominator in more than one way, recording each decomposition by an equation. Justify decompositions, e.g., by using a visual fraction model. Examples: \( \frac{3}{8} = \frac{1}{8} + \frac{1}{8} + \frac{1}{8} \); \( \frac{3}{8} = \frac{1}{8} + \frac{2}{8} \); \( \frac{2}{1/8} = \frac{1}{1/8} + \frac{1}{8} = \frac{8}{8} + \frac{8}{8} + \frac{1}{8} \).
Students should justify their breaking apart (decomposing) of fractions using visual fraction models. The concept of turning mixed numbers into improper fractions needs to be emphasized using visual fraction models.

Example:

\[
\begin{array}{c}
3/8 & = 1/8 + 1/8 + 1/8 \\
3/8 & = 1/8 + 2/8 \\
2 1/8 & = 1 + 1/8 \\
\text{or} \\
2 1/8 & - 8/8 + 8/8 + 1/8
\end{array}
\]

\[\text{Mixed numbers are introduced for the first time in 4th Grade. Students should have ample experiences of adding and subtracting mixed numbers where they work with mixed numbers or convert mixed numbers into improper fractions.} \]

Example:

Susan and Maria need 8 \(\frac{3}{8}\) feet of ribbon to package gift baskets. Susan has 3 \(\frac{1}{8}\) feet of ribbon and Maria has 5 \(\frac{3}{8}\) feet of ribbon. How much ribbon do they have altogether? Will it be enough to complete the project? Explain why or why not.

The student thinks: I can add the ribbon Susan has to the ribbon Maria has to find out how much ribbon they have altogether. Susan has 3 \(\frac{1}{8}\) feet of ribbon and Maria has 5 \(\frac{3}{8}\) feet of ribbon. I can write this as 3 \(\frac{1}{8}\) + 5 \(\frac{3}{8}\). I know they have 8 feet of ribbon by adding the 3 and 5. They also have \(\frac{1}{8}\) and \(\frac{3}{8}\) which makes a total of \(\frac{4}{8}\) more. Altogether they have 8 \(\frac{4}{8}\) feet of ribbon. 8 \(\frac{4}{8}\) is larger than 8 \(\frac{3}{8}\) so they will have enough ribbon to complete the project. They will even have a little extra ribbon left: \(\frac{1}{8}\) foot.

Example:

Trevor has 4 \(\frac{3}{8}\) pizzas left over from his soccer party. After giving some pizza to his friend, he has \(2 \frac{4}{8}\) of a pizza left. How much pizza did Trevor give to his friend?

Possible solution: Trevor had 4 \(\frac{1}{8}\) pizzas to start. This is \(\frac{33}{8}\) of a pizza. The x’s show the pizza he has left which is \(2 \frac{4}{8}\) pizzas or \(\frac{20}{8}\) pizzas. The shaded rectangles without the x’s are the pizza he gave to his friend which is \(\frac{13}{8}\) or \(1 \frac{5}{8}\) pizzas.
While solving the problem, \(3\frac{3}{4} + 2\frac{1}{4}\), students could do the following:

**Student 1:** \(3 + 2 = 5\) and \(\frac{3}{4} + \frac{1}{4} = 1\), so \(5 + 1 = 6\).

**Student 2:** \(3\frac{3}{4} + 2 = 5\frac{3}{4}\), so \(5\frac{3}{4} + \frac{1}{4} = 6\).

**Student 3:** \(3\frac{3}{4} = \frac{15}{4}\) and \(2\frac{1}{4} = \frac{9}{4}\), so \(\frac{15}{4} + \frac{9}{4} = \frac{24}{4} = 6\).

d. Solve word problems involving addition and subtraction of fractions referring to the same whole and having like denominators, e.g., by using visual fraction models and equations to represent the problem.

Example:

A cake recipe calls for you to use \(\frac{3}{4}\) cup of milk, \(\frac{1}{4}\) cup of oil, and \(\frac{2}{4}\) cup of water. How much liquid was needed to make the cake?

**MGSE4.NF.4** Apply and extend previous understandings of multiplication to multiply a fraction by a whole number.

a. Understand a fraction \(a/b\) as a multiple of \(1/b\). For example, use a visual fraction model to represent \(5/4\) as the product \(5 \times (1/4)\), recording the conclusion by the equation \(5/4 = 5 \times (1/4)\).

This standard builds on students’ work of adding fractions and extending that work into multiplication.

Example: \(\frac{3}{6} = \frac{1}{6} + \frac{1}{6} + \frac{1}{6} = 3 \times \frac{1}{6}\)

**Number line:**

**Area model:**
b. Understand a multiple of $a/b$ as a multiple of $1/b$, and use this understanding to multiply a fraction by a whole number. For example, use a visual fraction model to express $3 \times (2/5)$ as $6 \times (1/5)$, recognizing this product as $6/5$. (In general, $n \times (a/b) = (n \times a)/b$.)

This standard extended the idea of multiplication as repeated addition. For example, $3 \times \frac{2}{5} = \frac{2}{5} + \frac{2}{5} + \frac{2}{5} = \frac{6}{5} = 6 \times \frac{1}{5}$.

Students are expected to use and create visual fraction models to multiply a whole number by a fraction.

\[
\begin{array}{c}
\frac{1}{5} \quad \frac{2}{5} \quad \frac{3}{5} \quad \frac{4}{5} \quad \frac{5}{5} \\
\hline
\frac{1}{5} \quad \frac{2}{5} \quad \frac{3}{5} \quad \frac{4}{5} \quad \frac{5}{5}
\end{array}
\]

\[
\begin{array}{c}
\frac{2}{5} \quad \frac{3}{5} \quad \frac{4}{5} \quad \frac{5}{5} \\
\hline
\frac{1}{5} \quad \frac{2}{5} \quad \frac{3}{5} \quad \frac{4}{5} \quad \frac{5}{5}
\end{array}
\]

\[
\begin{array}{c}
\frac{3}{5} \quad \frac{4}{5} \quad \frac{5}{5} \\
\hline
\frac{1}{5} \quad \frac{2}{5} \quad \frac{3}{5} \quad \frac{4}{5} \quad \frac{5}{5}
\end{array}
\]

\[
\begin{array}{c}
\frac{4}{5} \quad \frac{5}{5} \\
\hline
\frac{1}{5} \quad \frac{2}{5} \quad \frac{3}{5} \quad \frac{4}{5} \quad \frac{5}{5}
\end{array}
\]

c. Solve word problems involving multiplication of a fraction by a whole number, e.g., by using visual fraction models and equations to represent the problem. For example, if each person at a party will eat $3/8$ of a pound of roast beef, and there will be 5 people at the party, how many pounds of roast beef will be needed? Between what two whole numbers does your answer lie?

This standard calls for students to use visual fraction models to solve word problems related to multiplying a whole number by a fraction.

Example:
In a relay race, each runner runs $\frac{3}{8}$ of a lap. If there are 4 team members how long is the race?

**Student 1** – Draws a number line showing 4 jumps of $\frac{3}{8}$:

\[
\begin{array}{c}
\frac{3}{8} \quad \frac{3}{8} \quad \frac{3}{8} \quad \frac{3}{8}
\end{array}
\]

**Student 2** – Draws an area model showing 4 pieces of $\frac{3}{8}$ joined together to equal 2:

\[
\begin{array}{c}
\frac{3}{8} \quad \frac{3}{8}
\end{array}
\]

\[
\begin{array}{c}
\frac{3}{8} \quad \frac{3}{8}
\end{array}
\]

**Student 3** – Draws an area model representing $4 \times \frac{3}{8}$ on a grid, dividing one row into $\frac{3}{8}$ to represent the multiplier:

\[
\begin{array}{c}
\frac{3}{8} \quad \frac{3}{8}
\end{array}
\]

Example:
Heather bought 12 plums and ate $\frac{13}{12}$ of them. Paul bought 12 plums and ate $\frac{14}{12}$ of them. Which statement is true? Draw a model to explain your reasoning.

a. Heather and Paul ate the same number of plums.

b. Heather ate 4 plums and Paul ate 3 plums.

c. Heather ate 3 plums and Paul ate 4 plums.

d. Heather had 9 plums remaining.
Examples:
Students need many opportunities to work with problems in context to understand the connections between models and corresponding equations. Contexts involving a whole number times a fraction lend themselves to modeling and examining patterns.

1. \[3 \times \frac{2}{5} = 6 \times \frac{1}{5} = \frac{6}{5}\]

2. If each person at a party eats \(\frac{3}{8}\) of a pound of roast beef, and there are 5 people at the party, how many pounds of roast beef are needed? Between what two whole numbers does your answer lie?
A student may build a fraction model to represent this problem:

\[
\begin{align*}
\frac{3}{8} & \quad \frac{3}{8} \\
\frac{3}{8} & \quad \frac{3}{8} \\
\frac{3}{8} & \quad \frac{3}{8} \\
\frac{3}{8} & \quad \frac{3}{8}
\end{align*}
\]

\[
\frac{3}{8} + \frac{3}{8} + \frac{3}{8} + \frac{3}{8} + \frac{3}{8} = \frac{15}{8} = 1 \frac{7}{8}
\]

Common Misconceptions
Students think that it does not matter which model to use when finding the sum or difference of fractions. They may represent one fraction with a rectangle and the other fraction with a circle. They need to know that the models need to represent the same whole.

MGSE4.MD.4 Make a line plot to display a data set of measurements in fractions of a unit (1/2, 1/4, 1/8). Solve problems involving addition and subtraction of fractions by using information presented in line plots. For example, from a line plot find and interpret the difference in length between the longest and shortest specimens in an insect collection.

This standard provides a context for students to work with fractions by measuring objects to an eighth of an inch. Students are making a line plot of this data and then adding and subtracting fractions based on data in the line plot.
Example:
Students measured objects in their desk to the nearest 1/2, 1/4, or 1/8 inch. They displayed their data collected on a line plot. How many objects measured 1/4 inch? 1/2 inch? If you put all the objects together end to end what would be the total length of all the objects.

Common Misconceptions
Students use whole-number names when counting fractional parts on a number line. The fraction name should be used instead. For example, if two-fourths is represented on the line plot three times, then there would be six-fourths.
MGSE4.OA.3 Solve multistep word problems posed with whole numbers and having whole-number answers using the four operations, including problems in which remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.

The focus in this standard is to have students use and discuss various strategies. It refers to estimation strategies, including using compatible numbers (numbers that sum to 10 or 100) or rounding. Problems should be structured so that all acceptable estimation strategies will arrive at a reasonable answer.

Example 1:
On a vacation, your family travels 267 miles on the first day, 194 miles on the second day and 34 miles on the third day. How many miles did they travel total?

Some typical estimation strategies for this problem are shown below.

<table>
<thead>
<tr>
<th>Student 1</th>
<th>Student 2</th>
<th>Student 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>I first thought about 267 and 34. I noticed that their sum is about 300. Then I knew that 194 is close to 200. When I put 300 and 200 together, I get 500.</td>
<td>I first thought about 194. It is really close to 200. I also have 2 hundreds in 267. That gives me a total of 4 hundreds. Then I have 67 in 267 and the 34. When I put 67 and 34 together that is really close to 100. When I add that hundred to the 4 hundreds that I already had, I end up with 500.</td>
<td>I rounded 267 to 300. I rounded 194 to 200. I rounded 34 to 30. When I added 300, 200, and 30, I know my answer will be about 530.</td>
</tr>
</tbody>
</table>

The assessment of estimation strategies should only have one reasonable answer (500 or 530), or a range (between 500 and 550). Problems will be structured so that all acceptable estimation strategies will arrive at a reasonable answer.

Example 2:
Your class is collecting bottled water for a service project. The goal is to collect 300 bottles of water. On the first day, Max brings in 3 packs with 6 bottles in each container. Sarah wheels in 6 packs with 6 bottles in each container. About how many bottles of water still need to be collected?

<table>
<thead>
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<th>Student 1</th>
<th>Student 2</th>
</tr>
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<tbody>
<tr>
<td>First I multiplied 3 and 6 which equals 18. Then I multiplied 6 and 6 which is 36. I know 18 plus 36 is about 50. I’m trying to get to 300. 50 plus another 50 is 100. Then I need 2 more hundreds. So we still need 250 bottles.</td>
<td>First I multiplied 3 and 6 which equals 18. Then I multiplied 6 and 6 which is 36. I know 18 is about 20 and 36 is about 40. 40 + 20 = 60. 300 – 60 = 240, so we need about 240 more bottles.</td>
</tr>
</tbody>
</table>

This standard references interpreting remainders. Remainders should be put into context for interpretation. Ways to address remainders:

- Remain as a left over
- Partitioned into fractions or decimals
- Discarded leaving only the whole number answer
- Increase the whole number answer up one
- Round to the nearest whole number for an approximate result

Example:
Write different word problems involving $44 \div 6 = ?$ where the answers are best represented as:

- Problem A: 7
• Problem B: 7 r 2
• Problem C: 8
• Problem D: 7 or 8
• Problem E: $7^2/6$

Possible solutions:

• Problem A: 7.
  Mary had 44 pencils. Six pencils fit into each of her pencil pouches. How many pouches did she fill? $44 \div 6 = p; p = 7 r 2$. Mary can fill 7 pouches completely.

• Problem B: 7 r 2.
  Mary had 44 pencils. Six pencils fit into each of her pencil pouches. How many pouches could she fill and how many pencils would she have left? $44 \div 6 = p; p = 7 r 2$; Mary can fill 7 pouches and have 2 left over.

• Problem C: 8.
  Mary had 44 pencils. Six pencils fit into each of her pencil pouches. What would the fewest number of pouches she would need in order to hold all of her pencils? $44 \div 6 = p; p = 7 r 2$; Mary can needs 8 pouches to hold all of the pencils.

• Problem D: 7 or 8.
  Mary had 44 pencils. She divided them equally among her friends before giving one of the leftovers to each of her friends. How many pencils could her friends have received? $44 \div 6 = p; p = 7 r 2$; some of her friends received 7 pencils. Two friends received 8 pencils.

• Problem E: $7^2/6$.
  Mary had 44 pencils and put six pencils in each pouch. What fraction represents the number of pouches that Mary filled? $44 \div 6 = p; p = 7^2/6$
  Example:
  There are 128 students going on a field trip. If each bus held 30 students, how many buses are needed? $(128 \div 30 = b; b = 4 R 8$; they will need 5 buses because 4 busses would not hold all of the students).

Students need to realize in problems, such as the example above, that an extra bus is needed for the 8 students that are left over. Estimation skills include identifying when estimation is appropriate, determining the level of accuracy needed, selecting the appropriate method of estimation, and verifying solutions or determining the reasonableness of situations using various estimation strategies. Estimation strategies include, but are not limited to the following.
  • **Front-end estimation with adjusting** (Using the highest place value and estimating from the front end, making adjustments to the estimate by taking into account the remaining amounts)
  • **Clustering around an average** (When the values are close together an average value is selected and multiplied by the number of values to determine an estimate.)
  • **Rounding and adjusting** (Students round down or round up and then adjust their estimate depending on how much the rounding affected the original values.)
  • **Using friendly or compatible numbers such as factors** (Students seek to fit numbers together; e.g., rounding to factors and grouping numbers together that have round sums like 100 or 1000.)
  • **Using benchmark numbers that are easy to compute** (Students select close whole numbers for fractions or decimals to determine an estimate.)

(Adapted from Henry County Schools)